Stability of Colloids in Negatively Co-operative Melittin–Phospholipid

Estabilidad de los coloides en la interacción negativa melitina-fosfolípido

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ABSTRACT

The adsorption of melittin on 1-palmitoyl-2-oleoyl-sn-glycero-3-phosphocholine membranes is analysed. Rising melittin concentration, a multilayer adsorption is observed and discussed in terms of either monomer or tetramer stacking to the surface. An electrostatic adsorption model is applied because of the cationic peptide. According to the Derjaguin–Landau–Verwey–Overbeek theory, the energy well corresponding to melittin aggregation in membranes is rather broad and, practically, no barrier exists opposing the aggregation of melittin molecules. Such aggregation corresponds to a small energy variation relative to the thermal energy, which suggests that spontaneous thermal fluctuations can affect the aggregation state of melittin at the membrane–solution interface. The results of the work make evident the multilayer formation of melittin on phospholipid membranes. Melittin tetramers, which are formed in solution, bind directly to the phospholipid membrane, which results in multilayers on the surface. Adsorption is treated via Langmuir adsorption isotherm modified by electrostatic effects. The theoretical treatment is an elegant method because both Gouy–Chapman and Debye–Hückel formalisms apply Poisson–Boltzmann equation to calculate the potential.

KEYWORDS: Peptide-lipid interaction, Thermodynamic treatment, Binding isotherm, Scatchard plot, Hill plot.

RESUMEN

Se analiza la adsorción de melitina sobre membranas de 1-palmitoil-2-oleoil-sn-glicero-3-fosfolipido. Elevando la concentración de melitina, se observa y discute una adsorción en multilaminas en cuanto a apilamiento, bien de monómeros, bien de tetrameras, hacia la superficie. Se aplica un modelo de adsorción electrostática por el péptido catiónico. De acuerdo con la teoría Derjaguin-Landau-Verwey-Overbeek, el pozo de energía que corresponde a la agregación de melitina en membranas es bastante ancho, y prácticamente no existe barrera que se oponga a la agregación de moléculas de melitina. Tal agregación corresponde a una pequeña variación de energía relativa a la energía térmica, que sugiere que espontáneas fluctuaciones térmicas pueden afectar al estado de agregación de la melitina en la interfase membrana-disolución. Los resultados del trabajo evidencian la formación de multilaminas de melitina sobre membranas fosfolipídicas. Tetrameras de melitina, que se forman en disolución, enlanzan directamente con la membrana
fosfolípídica, que resulta en multicapas sobre la superficie. La adsorción se trata vía la isoterma de adsorción de Langmuir, modificada por efectos electrostáticos. El tratamiento teórico es un elegante método porque los formalismos tanto de Gouy-Chapman como Debye-Hückel aplican la ecuación de Poisson-Boltzmann para calcular el potencial.

**PALABRAS CLAVE:** Interacción péptido-lípido, tratamiento termodinámico, isoterma de enlace, Diagrama de Scatchard, Diagrama de Hill.

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**INTRODUCTION**

Studies on the interactions between membranes and peptides are central to the knowledge of the insertion process of membrane proteins, binding of hormones to membrane receptors, and action of antimicrobial peptides (AMPs) and toxins. The general principles of the mechanism of interaction of surface-active peptides with membranes are understood, but the details necessary for a quantitative structure–activity and thermodynamic frameworks remain elusive. Melittin is the main active component (52 % of venom peptides) of apitoxin (European honey bee Apis mellifera venom) and is a powerful stimulator of phospholipase A2 (PLA2). It is a linear, basic, amphiphilic, cytotoxic, cytolytic and haemolytic oligopeptide with 26 amino acids (AAs) and the sequence H$_3$N$^+$–GIGAVLV- LTTGLPALISWKIRKRQQ–CONH$_2$ (molecular weight $M_w$=2846g·mol$^{-1}$). Sequences of hydrophobic (1–20) and hydrophilic (21–26) AAs are unequally distributed. It presents strong amphipathic surface activity, and is known to adopt a number of conformations and aggregation states in different aqueous solutions. Its conformation is largely random coil (disordered) when present as free monomer in solution. Melittin binds to cell membranes, causing their lysis vía not completely understood mechanisms. The aggregation state and orientation of its amphipathic $\alpha$–helix with respect to the membrane remain controversial. It adopts an amphipathic $\alpha$–helical conformation when bound to membranes and micelles, with a flexible hinge in Pro$^{14}$ and unordered C-terminal at 22–26 AAs. The Pro$^{14}$ plays a critical role in its antimicrobial activity and cytotoxicity. At high peptide concentration or ionic strength, it self-associates into a tetrameric structure. The relationship between the tetrameric self-assembly of melittin and its bioactivity was linked to the necessity to prevent its hydrophobic residues from being exposed to the sugar charges present in biomembranes. Although it presents mainly hydrophobic residues, it shows six positive charges. Its N-terminal part is hydrophobic while C-end moiety is hydrophilic and strongly basic.

In order to understand membrane-lysis mechanism induced by melittin, effectors microscopic localization in the membranes at physiological concentrations is needed. Melittin orientation with respect to the bilayer surface is parallel or perpendicular, depending on the used lipid and hydration extent. Its amphiphilic nature resembles membrane-bound peptides, apolipoproteins and putative transmembrane helices of membrane proteins, which resulted in melittin being used as a model of lipid–protein interactions, toxin-mediated membrane disruption and ion channel-forming proteins. Its characteristic effect on cell membranes is the ability to lyse natural and artificial ones. It disrupts gel-phase zwitterionic 1-palmitoyl-2-oleoyl-sn-glycero-3-phosphocholine (POPC) membranes into small discoidal objects, with diameter of 200–400Å and a thickness of a single bilayer. In flu-
id-phase POPC bilayers, it induces the formation of large unilamellar vesicles (LUVs) with diameter of 2000Å. Because of its cationic charge, melittin binds distinctly more to anionic than zwitterionic bilayers. Studies on anions influence on melittin action were performed on binary bilayer systems of POPC and anionic lipids [e.g., 1-palmitoyl-2-oleoyl-sn-glycero-3-phosphatidylserine (PS), 1-palmitoyl-2-oleoyl-sn-glycero-3-phosphoglycerol (POPG)], which present the inconvenience that it is difficult to distinguish if melittin interacts with the initially provided mixture or domains locally enriched in one compound. Is glutaminyl-substrate melittin a model peptide substrate to explore membrane-phospholipids role on the enzymatic activity of tissue transglutaminase (tTGase)?

Work showed that bee venom presents multiple effects, probably as a result of its interaction with anionic phospholipids. Melittin increases the permeability of cell membranes to ions (e.g., Na⁺, Ca²⁺, Cl⁻), which effect causes morphological (e.g., swelling), and functional changes in cells and tissues. Melittin exhibits antimicrobial activity vs. Borrelia burgdorferi, Candida albicans, Mycoplasma hominis, Chlamydia trachomatis, etc. Habermann reviewed bee and wasp venoms [1]. Properties of AMPs were reviewed [2–21]. A special issue of Current Topics in Medicinal Chemistry was edited on AMPs [22]. Differential AMPs interaction with lipid structures were studied by coarse-grained molecular dynamics simulations [23]. Analysis of antimicrobial activities in relation to amphipathicity and charge characterized antimicrobial peptides [24]. Work on AMP analogues from scorpion venom, antimicrobial activity and toxicity showed that α-helix interacted with biomembranes according to carpet, toroidal and barrel models, and aggregates formed with rising concentration.

In an earlier publication, it was informed the binding of vinyl polymers to anionic model membranes [25], the interaction of polyelectrolytes with oppositely charged micelles studied by fluorescence and liquid chromatography [26], the negatively co-operative binding of melittin to neutral phospholipid vesicles, the stability of pairs of colloidal particles [Derjaguin–Landau–Verwey–Overbeek (DLVO) theory] [27], the binding of water-soluble, globular proteins to anionic model membranes [28], the comparative analysis of the electrostatics of the binding of cationic proteins to vesicles, the asymmetric location of anionic phospholipids [29], the binding of mono, bi and tridomain proteins to zwitterionic and anionic vesicles, the asymmetric location of anionic phospholipids in mixed zwitterionic/anionic vesicles and the co-operative binding [30]. In Nereis, it was reported the polymer bisphenol-A (BPA), incorporation of silica (SiO₂) nanospheres (nanosilica, nano-SiO₂) into epoxy/amine materials, polymer nanocomposites (NCs) [31] and the calculation of restricted volume for nanoparticles that can point [32]. In the present report, the condition of DLVO stability for colloids is reviewed. The aim is to investigate if the peptide–phospholipid binding model is generally valid and determine what is the driving force for the interaction: the net surface charge density, lipid physical state or its inverse hexagonal phase (H₃)-promoting character. The purpose is to examine the stability of thermosetting polymer/nanoclay dispersions. The main objective is to analyze the adsorption of melittin on zwitterionic lipid POPC membranes. Rising melittin concentration, a multilayer adsorption is observed and discussed in terms of monomer or tetramer stacking to the surface.
METHOD

Condition of Stability for Colloids (Derjaguin–Landau–Verwey–Overbeek Theory)

Colloids

Colloids can be classified according to the nature [gas (G), liquid (L), solid (S)] of the dispersed phase (approximately spherical fragments of size varying in 10–10^4 Å) and that of the dispersive milieu. Table 1 gives some examples of colloidal systems after this classification.

<table>
<thead>
<tr>
<th>Table 1. Classification of colloidal systems and examples</th>
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<tr>
<td>Class</td>
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<tr>
<td>1. Liquid aerosols</td>
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<tr>
<td>2. Solid aerosols</td>
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<tr>
<td>3. Foams</td>
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<td>4. Emulsions</td>
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<td>5. Colloidal suspensions (sols)</td>
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<tr>
<td>6. Solid foams</td>
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<tr>
<td>7. Solid emulsions (gels)</td>
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<td>8. Solid suspensions</td>
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<sup>a</sup>L: liquid.
<sup>b</sup>S: solid.
<sup>c</sup>G: gas.

The most important class, corresponding to Entry 5 (colloidal suspensions, sols), splits into two categories: (1) hydrophilic (lyophilic) colloids where properties (viscosity coefficient, surface tension) are different from the dispersive milieu (sol ↔ gel, e.g., gelatine in H₂O); (2) hydrophobic (lyophobic) colloids where the properties look like the dispersive milieu; such colloids are pH-sensitive and present an instability (flocculation) for a pH higher than a critical value (e.g., colloidal Au). Derjaguin–Landau–Verwey–Overbeek (DLVO) theory is devoted to lyophobic-colloids stability [33,34].

Interaction between Two Charged Spheres

The problem of the repulsive force from electrostatic origin between two charged spheres is much more difficult to solve than that of the potential originated from one charged sphere. No simple expression of the corresponding potential exists but reasonable approximations are known for limit situations [35]; e.g., for two identical spheres of radius \( a \) in a milieu characterized by the Debye length \( \lambda_D = 1/\kappa = (e k T / 8 \pi \varepsilon^2 n^\circ)^{1/2} \) [where \( \varepsilon \) is the solvent permittivity (before the introduction of the ions), \( k \),
Boltzmann constant, $T$, the absolute temperature, $e$, the proton charge, and $n^o$, the number of ions per unit volume in the absence of any charged surface], one obtains:

$$V_{el} = \frac{eay^2}{2} \exp(-ks)$$  \hspace{1cm} (1)

where $s$ is the shortest distance between the surfaces of the spheres in presence ($s \ll a$), and $\psi$, a potential characterizing both the charge state of the spheres and the properties of the ions of the intermediate milieu.

**Total Interaction between Two Charged Spheres in an Ionized Milieu**

The van der Waals (VdW) energy (attractive for two spheres presenting the same chemical composition) is:

$$V(D) = -\frac{AR}{12D}$$  \hspace{1cm} (2)

where $R$ is the radius of both spheres, $D$, the minimum distance between both spherical surfaces, $A$, the Hamaker constant ($A = \pi^2 n^2 B$), $n$, the number of spheres per unit volume, $B$, the attractive interaction constant of London in $r^{-6}$ between an atom of sphere 1 and an atom of sphere 2, and $r$, the interatomic distance. The total interaction energy between two charged spheres in an ionized milieu is obtained, in DLVO framework, joining Eqs. (2) and (1) corresponding, respectively, to VdW and electrostatic energy (repulsive for approaching distances lower than $\lambda_D$, practically null farther). Therefore,

$$V = -\frac{Aa}{12s} + \frac{eay^2}{2} \exp(-ks)$$  \hspace{1cm} (3)

This expression will be used to discuss the stability of a colloid suspension.

**Stability of a Pair of Colloidal Particles**

In a colloidal suspension of lyophobic type, system flocculation is expected when the attractive forces between two particles dominate over the repulsive ones. Potential function between two charged spheres given by Eq. (3) will be written:

$$V(s) = V_A(s) + V_R(s)$$  \hspace{1cm} (4)

Notice after Eq. (3) that absolute $V_R$ is small with respect to $V_A$ as for both $s \sim 0$ and $s \rightarrow \infty$. However, both cases in Fig. 1 are possible.
(1) In Fig. 1a, the repulsive effects are sufficiently intense in order that a maximum appear for $V(s)$, which corresponds to an activation energy needed for the two spheres to become in contact ($s = 0$). For a colloidal system, the figure corresponds to a possible *stability*. (2) However, in the case of Fig. 1b, $V_R$ is too weak in order that the maximum would appear, and the figure corresponds to an immediate *flocculation* of the colloid. Figure 2 represents the net of curve $V = V(s)$ for different values of the inverse Debye length $\kappa$ of the ionic milieu.

![Fig. 1. Interaction potential vs. distance between particles: (a) domain of repulsive effects; (b) domain of attractive effects.](image)

![Fig. 2. Representation of the net of curve $V = V(s)$ for different values of the Debye length $\kappa^{-1}$ of the ionic milieu.](image)
One can go further searching for the condition by which curve $V = V(r)$ present a maximum and a minimum. Equation (3) can thus be rewritten, measuring $s$ in $\lambda_\eta$ units, i.e., taking $s = \sigma/\kappa$:

$$V(\sigma) = -\frac{A\kappa}{12\sigma} + \frac{\varepsilon\psi^2}{2} \exp(-\sigma)$$  \hspace{1cm} (5)

Nullifying the derivative of this expression:

$$\frac{dV}{d\sigma} = \frac{A\kappa}{12\sigma^2} - \frac{\varepsilon\psi^2}{2} \exp(-\sigma) = 0$$  \hspace{1cm} (6)

Thus:

$$\sigma^2 \exp(-\sigma) = \frac{A\kappa}{6\varepsilon\psi^2}$$  \hspace{1cm} (7)

The $y(\sigma) = \sigma^2 \exp(-\sigma)$ function is represented in Fig. 3.

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Fig. 3. Representation of the $y(\sigma) = \sigma^2 \exp(-\sigma)$ function vs. $\sigma$.

The figure above shows that if:

$$\frac{A\kappa}{6\varepsilon\psi^2} > \frac{4}{\exp(2)} = 0.5413$$  \hspace{1cm} (8)
then $V = V(r)$ curve presents no extreme. In this case, the attractive VdW force dominates, whichever $s$ be, over the electrostatic repulsion and the colloid is unstable. Inequality (8) can also be written:

$$\psi^2 < \psi_{\text{crit}}^2 = \frac{AK}{24\varepsilon}\exp(2)$$

(9)

For a millimolar aqueous solution of monovalent ions, one has $\psi_{\text{crit}} = 19\text{mV}$. When $V = V(r)$ presents a maximum, i.e., if $\psi > \psi_{\text{crit}}$, one can search for the value of $V$ that correspond to the maximum. It matches to a value of $\sigma_o$ of $\sigma$ so that:

$$\exp(-\sigma_o) = \frac{AK}{6\varepsilon}\frac{\psi^2_{\text{crit}}}{\sigma_o^2}$$

(10)

From which:

$$V(\sigma_o) = \frac{AKa}{12\sigma_o} + \frac{\varepsilon\psi^2}{2}\exp(-\sigma_o) = -\frac{AKa}{12\sigma_o} + \frac{AKa}{12\sigma_o^2} = \frac{AKa}{12\sigma_o}\left(1 - \frac{1}{\sigma_o}\right)$$

(11)

Let us assume $\psi >> \psi_{\text{crit}}$, then $\sigma_o^2\exp(-\sigma_o) = AK/(6\varepsilon\psi^2) << 1$, and $\sigma_o << 1$. From which:

$$V(\sigma_o) = \frac{AKa}{12\sigma_o} = \frac{\varepsilon\psi^2}{2}$$

(12)

For instance, if $a = 0.5\mu\text{m}$, $\varepsilon_w = 80$ (aqueous solution, $\varepsilon = \varepsilon_w\varepsilon_o = 7 \times 10^{-10}\text{C}^2\cdot\text{N}^{-1}\cdot\text{m}^{-2}$), $\psi = 100\text{mV}$, then $V(\sigma_o) = 2.2 \times 10^{-17}\text{J}$. At room temperature (RT) one obtains:

$$\frac{V(\sigma_o)}{kT} = 5000$$

In the conditions above, the activation energy is 5000 times higher than the average thermal agitation energy. One can then consider that one collision out of $\exp(5000) \approx 10^{2000}$ will cause the coalescence of the two concerned colloidal particles. The suspension could then be considered stable (flocculation of the colloid cannot occur).

**Stability of Thermosetting Polymer/Nanoclay Dispersions**

The term *stability* presents two meanings in the context of colloidal dispersions. In practice, it is used to show that there is no phase separation during a period. If the particles in a dispersion show a trend to sediment during an episode of storage, the dispersion is unstable. However, in another context, the word *stability* is utilized when the particles do not show a tendency to aggregate. The key to understand the expression *colloidal stability* is in the pair of potentials existing between two parti-
cles. The colloidal particles are subjected to attraction and repulsion forces, and an equilibrium exists between such forces. Brownian motion produces collision between the particles and, if the attraction forces dominate, the particles agglomerate after the impact. On the contrary, if the repulsion forces prevail, the particles remain separate after the collision. The attraction forces are those of VdW, while the repulsion forces come from the interaction between the electric double layers that enclose the particles. Variations of milieu ionic strength or pH modify electrostatic forces, which allows controlling co-agulation processes. Theory of DLVO developed the research, which gives total potential $V_T$ as:

$$V_T = V_A + V_R$$  \hspace{1cm} (13)

where $V_T$ is total potential between two particles as the addition of attraction $V_A$ and repulsion $V_R$ potentials. The curve that represents the total energy of interaction between colloidal particles ($V_T$) is the adding of attraction ($V_A$) and repulsion ($V_R$) curves. It corresponds to an exponential equation, because repulsion force is inversely proportional to the square of distance, and the attraction force is also a function of the inverse of distance but this raised to an exponent always greater than two. When the attraction by VdW forces is greater than the electrostatic repulsion, one is in the primary minimum potential (cf. Fig. 4), which indicates the aggregation state of the particles with the condition of minimum energy. The state of primary maximum represents the activation energy necessary to reach the aggregation state. Movement of the particles is governed by the thermal energy and, naturally, one can describe the energy distribution after Boltzmann equation. One can predict the kinetic stability as aggregation rate, being proportional to: $\exp(-V_T/k_BT)$. When $V_T >> k_BT$, the particles will be in a stable colloidal state. If the attraction energy is slightly greater than the thermal energy average, the aggregation states will be reversible (secondary minimum state). If a strong attraction exists between the particles, one has $-V_T >> k_BT$, and get a strong aggregation or co-agulation of the particles, resulting the process irreversible (primary minimum state).

![Fig. 4. Interaction potential vs. distance between the particles.](image)
On rising particle concentration in the milieu, the aggregates grow in size, adopting a fractal-type structure. Russel et al. described the phenomenon [36]. The aggregates grow and occupy the whole available space. In this point, the percolation threshold is reached. When rising particle concentration, the aggregates grow forming clusters that, in turn, interact with one another producing a continuous structure crosslinked (net) in three dimensions (3D). From this point, on rising particle concentration, dense structures are formed, which are more difficult to describe from an only parameter, e.g., fractal dimension. Gelification corresponds, at the molecular level, to the incipient formation of branched and reticulated molecules of a molecular weight that tends to infinite, insoluble and infusible. When gelification occurs, the system passes from liquid to a covalently interwoven gel. The phenomenon is associated with a sharp rise in the viscosity coefficient. From the theoretical viewpoint, the gel point was described via predictions of the classical polymerization theory developed by Flory [37] to modern fractal geometry [38] and percolation theory [39]. The theories contributed different explanations for the critical transition. Flory theory is incomplete because it does not consider the formation of rings, which implies that the mass of the fractal set rises with the fourth power of size, which is not realistic. Percolation theory allows the formation of rings, or closed cycles, so that it does not predict a divergent density for the fractal set. The validity of percolation theory lies in its ability to predict the behaviour of certain physical properties near the gel point [storage (elastic) modulus, viscosity coefficient, cluster average size and size distribution, gel volume fraction, etc.] via scaling laws governed by critical exponents. Fractal geometry is based on a structure invariant to scale (a part is structurally identical to the total) and shows a decay in density with the rise in aggregates size. Fractal objects are characterized by their fractal dimension $D$, which is defined from the fractal mass and surface by the following relationships:

\[ M \sim R^{D_m} \quad S \sim R^{D_s} \]  

where $M$ and $S$ are the object mass and surface, and $R$, its average size. Fractal mass and surface can never be in the same length scale. Index $D_m$ takes values in 1–3. The values result from $D_m = 1–1.5$, which corresponds to a long linear polymer, passing by $D_m = 1.5–2.25$ for branched and dendritic polymers to dense aggregates with $D_m \sim 3$. On the other hand, the values of $D_s$ rise from $D_s \sim 2$ for a smooth surface to $D_s \sim 3$ for a wrinkled surface. Shih et al. theory (1990) explained the formation of a continuous colloidal structure, crosslinked by interaction between the fractal flocs, distinguishing between two regimes according to colloidal-gel concentration [40,41]. It is important to determine the dependence of the storage shear modulus $G'$ on clay volume fraction $\phi$, in order to understand the mechanism controlling net-structure formation. Depending on the strength of the links between the flocs in comparison to that of the flocs, two regimes occur.

1. **Strong-link** regime, where:

\[ G \sim \phi^{(d+2)(d-D)} \]  

(15)
where $d$ is the Euclidean dimension, $D$, fractal dimension of the flocs, and $x$, backbone fractal dimension (chemical length exponent, tortuosity) of the flocs ($1 \leq x < D$). The limit of linearity (critical strain):

$$\gamma_c \sim \phi^{-(1 + x)(d - D)}$$

(16)

(2) Weak-link regime, where:

$$G' \sim \phi^{(d - 2)(d - D)}$$

(17)

and

$$\gamma_c \sim \phi^{d - D}$$

(18)

In the strong-link regime, the interaction force between the flocs overcomes the interaction forces from inside the same floc while, in the weak-link regime, the interaction force between the particles from inside the same floc overwhelms the forces between the flocs. The main differences between the two regimes are: (1) $G'$ rises more slowly in the weak- than in the strong-link regime; (2) the limit of linearity $\gamma_c$ rises with increasing particle concentration in the weak-link regime but decays with rising particle concentration in the strong-link regime. Extensions to the DLVO theory were informed. Bocquet et al. reported effective charge saturation in colloidal suspensions [42]. Chapot et al. published interaction between charged anisotropic macromolecules and applied it to rod-like polyelectrolytes [43].

**RESULTS**

The use of the partition equilibrium model, in combination with Gouy–Chapman formalism, provided an expression to generate theoretical association isotherms that depended on two adjustable parameters: (1) the theoretical partition coefficient $\Gamma$, calculated from the initial slope of the experimental curves; (2) the peptide effective interfacial charge $\gamma$. The experimental binding isotherms were fitted via $\Gamma$ and $\gamma$ parameters. The theoretical isotherms looked qualitatively similar to those obtained via the thermodynamic approach. Values of $\Gamma$ theoretically calculated for melittin were of the same order of magnitude than those derived from the fitting analysis, which means that for every binding isotherm, the evaluated actual peptide charge in solution $z_p^+$ originated a theoretical $\Gamma$ value similar to that obtained from the initial slope. However, with the present thermodynamic treatment, the determination of $\Gamma$ and $\gamma$ parameters was made separately, without any extrapolation from the experimental isotherm. Data on multilayer formation of melittin on solid-supported POPC membranes (cf. Table 2) show a small calculated surface charge density $\sigma$ in the range 0–12mC.m$^{-2}$, too small to avoid co-alescence [44]. Surface potential $\psi_o$ calculated via Gouy–Chapman theory lies in the range 0–16mV. As a first approximation, a value of ionic strength ($I$)-corrected water permittivity $\varepsilon_w = 77.3062 – 13.1601I = 76.8$ and $\alpha$–helix conformation for the peptide (disc surface charge distribution,
were used. It was shown by spectroscopy that in the presence of membrane-mimetic solvents and/or surfactants, melittin formed a partial α-helix [46–48]. The DLVO analysis allows calculating an activation energy for coalescence in the range of 0–38 J·mol⁻¹ or 0–0.02 units of kT at room temperature (T = 25 °C), which indicates that one collision of 1–1.02 will cause the co-alescence of adsorbed melittin molecules, which is in agreement with the fact that melittin aggregates in membranes predominantly in the form of tetramers. This supports the scenario of multilayer formation in which melittin tetramers, which are formed in solution, bind directly to the phospholipid membrane, which turns out to be in multilayers (double layers) on the surface, which is in contrast to observations with DOPC vesicles [49], confirming the importance of the experimental conditions [concentration of melittin, pH, temperature, ionic strength (salt concentration), etc.].

Table 2. Melittin–POPC binding (temperature T = 25 °C, ionic strength I = 0.04 mol·L⁻¹, pH 7.2)

| ñ |  |  |  |  |  |  |  |  |
|---|---|---|---|---|---|---|---|
| 0.00 | 0.00 | – | – | – | – | – | – |
| 1.60 | 4.40 | 2.25 | 3.4 | 1.2 | 3670 | 2 | 0.0007 | 1.0007 |
| 2.2 | 3.60 | 1.8 | 2.8 | 1.7 | 2080 | 1 | 0.0005 | 1.0005 |
| 3.8 | 5.54 | 2.8 | 4.2 | 2.7 | 2090 | 3 | 0.001 | 1.001 |
| 6.2 | 7.54 | 3.8 | 5.7 | 3.8 | 1980 | 5 | 0.002 | 1.002 |
| 7.3 | 8.18 | 4.1 | 6.1 | 4.3 | 1900 | 5 | 0.002 | 1.002 |
| 8.4 | 9.78 | 4.9 | 7.2 | 4.5 | 2170 | 7 | 0.003 | 1.003 |
| 11.2 | 12.08 | 6.1 | 8.8 | 5.3 | 2290 | 11 | 0.004 | 1.004 |
| 20.5 | 16.4 | 8.1 | 11.5 | 7.6 | 2150 | 19 | 0.008 | 1.008 |
| 26.8 | 18.9 | 9.3 | 13.0 | 8.8 | 2150 | 24 | 0.01 | 1.01 |
| 40.2 | 23.2 | 11.3 | 15.4 | 10.7 | 2170 | 34 | 0.01 | 1.01 |
| 66.9 | 24.8 | 11.9 | 16.2 | 16.6 | 1490 | 38 | 0.02 | 1.02 |

a Equilibrium melittin concentration in the bulk solution.
b Moles of bound melittin per mole of POPC.
c Surface charge density calculated according to Seelig, Allegrini and Seelig with \( A_L = 68 \text{Å}^2 \), \( A_p = 200 \text{Å}^2 \), and \( z_p^+ = 2.2 \) e.u.
d Surface potential calculated by means of Gouy–Chapman theory.
e Concentration of melittin at the binding plane calculated with \( z_p^+ = 2.2 \) e.u.
f Partition coefficient.
g Activation energy calculated with ionic strength-corrected water permittivity \( \varepsilon_w = 76.8 \) and \( a = 7 \text{Å} \).
h Activation energy in kT units, where \( k \) is Boltzmann constant.
i Number of collisions necessary for achieving one effective collision.

DISCUSSION

The adsorption of melittin on phospholipid vesicles is treated via Langmuir adsorption isotherm modified with electrostatic effects [50]. The theoretical approach is an elegant treatment, because the
two Gouy–Chapman and Debye–Hückel formalisms applied the same Poisson–Boltzmann equation to calculate either potential [51]. On comparing the adsorption of cationic melittin on zwitterionic and anionic phospholipid vesicles, the latter is more complex because of its greater cover of the surface, which allows raising three questions: (1) Does the phospholipid surface continue to be anionic after a great cover by the cationic peptide? (2) What is the actual charge of the anionic surface after the adsorption of the cationic peptide? (3) Is Langmuir-modified adsorption isotherm still valid? The theoretical association isotherms, generated from the values of the actual peptide charge in solution $z_p^+$, described satisfactorily the experimental data at lower ionic strength, and a number of parameters, included in the equation, were varied in order to better reproduce the experimental binding curves obtained at higher ionic strengths. The partition coefficient theoretically derived for melittin was similar to that deduced according to more classical binding analyses. The formalism allowed determining the values of the molar free energies for melittin in aqueous and lipid phases. Such an understanding of the thermodynamic parameters provided interesting information about the energetic of the peptide–lipid interactions. In the following, I shall provide a tentative model for the topology of melittin in two possible scenarios of multilayer formation on POPC membranes. A thermodynamic approach was proposed to analyse quantitatively the binding isotherms of peptides to model membranes. The main features of the treatment were: (1) a theoretical expression for the partition coefficient calculated from the molar free energies of the peptide in both aqueous and lipid phases; (2) an equation proposed by Stankowski to evaluate the activity coefficient of the peptide in the lipid phase; (3) Debye–Hückel equation that quantifies the activity coefficient of the peptide in the aqueous phase [52]. In order to assess the validity of the method, the interaction of basic amphipathic peptides was studied via steady-state fluorescence spectroscopy, which provides: (1) intensity (related to the abundance of the melittin–peptide complex); (2) blueshift (penetration of the hydrophobic part of melittin in the bilayer). The obtained $z_p^+$ charges were always found to be lower than the electrostatic charge expected from the number of ionizable groups in the cationic peptide ($q = 6$ e.u.) [53]. The $z_p^+$ charges were rationalized, considering that the peptide charged groups were strongly associated with the counterions in the buffer solution at a given ionic strength [54]. The partition coefficients theoretically derived via $z_p^+$ charges were in agreement with those deduced from Gouy–Chapman formalism [55]. From $z_p^+$ charges, the molar free energies for both free and lipid-bound states of the peptides were calculated.

The experimental activity coefficient was explained taking into account the electrostatic effects and $v$ charge, and the experimental binding isotherms were fitted via $\Gamma$ and $v$ parameters [56]. However, determined $v$ charges were also smaller than the electrostatic charge of the cationic peptide, which observation was understood when it was considered that the actual $z_p^+$ charge of the cationic polypeptide should decay, because of the screening effect of the counterions in the electrolyte solution, which provided a given ionic strength [57]. In order to explain the charge difference, theoretical treatments were reported, but the thermodynamic parameters involved in the peptide–surface interactions were not well defined for electrolytes greater than 1:1 [58]. A thermodynamic approach was proposed for the quantitative analysis of the peptide/lipid-surface binding isotherms. The treatment was based on the partition equilibrium model and introduced: (1) the theoretical expressions for the quantitative calculation of the molar free energies of the peptide in both aqueous and lipid phases, which allowed the evaluation of the partition coefficient; (2) the calculation of the activity coefficient.
via concepts from the virial approach and Debye–Hückel theory, with both disc and hemispheric surface charge distributions considered for the peptide-vesicle contact. All the proposed expressions were based on the knowledge of the actual peptide charge in solution \( z_p^+ \), which was different from the electrostatic charge of the cationic peptide. Once \( z_p^+ \) charge was known, \( \nu \) charges were derived via Gouy–Chapman theory. With the present thermodynamic treatment, the determination of theoretical partition coefficient \( \Gamma \) and \( \nu \) charge parameters was made separately, without any extrapolation from the experimental binding isotherm, which observation was understood when it was considered a disc surface charge distribution for the melittin/vesicle contact.

Some amount of high-molecular mass complexes of melittin with mainly anionic phospholipids existed. The interaction between cationic melittin and POPC vesicles/membranes presented four phases. (1) The initial interaction between melittin and vesicles/cells was merely electrostatic via the basic C-terminus, but melittin was not fully stabilized at the vesicle/membrane plane and remained in a low \( \alpha \)-helical conformation. (2) The next step after the electrostatic interaction was a melittin stabilization in the vesicle/membrane. Conformational changes were induced to yield a peptide–lipid complex showing the lowest possible energy state. (3) The insertion of melittin in the vesicle/bilayer induced a re-organization of the vesicle/membrane components, which facilitated the cytoplasm release and concomitant cell collapse. (4) After the lysis was completed, melittin was complexed with mainly anionic phospholipids. The agreement between the results, obtained with wasp venom peptide toxin mastoparan, and experimental results gotten for melittin and neuropeptide substance \( P \), supported that quantitative studies of the binding of amphipathic peptides to zwitterionic and anionic phospholipid membranes were achieved, via the thermodynamic approach, especially at lower ionic strength. However, at higher salt concentration, the thermodynamic treatment did not completely predict the shape of the curves at high surface cover, which was attributed to the fact that an average \( z_p^+ \) charge was assumed in all cases in the calculations, as representative of the whole adsorption isotherm. At lower ionic strength, \( z_p^+ \) charges in every point of the adsorption isotherm were similar and an average \( <z_p^+> \) charge were adequate. Notwithstanding, at higher salt concentration, \( z_p^+ \) charges calculated for every experimental datum in the corresponding adsorption isotherm varied slightly, and the average \( z_p^+ \) charge was considered as a less representative parameter of the whole adsorption isotherm, which could be corrected introducing, in the theoretical expression of the molar free energies of the peptide in both aqueous and lipid phases, additional terms accounting for the interaction between the free peptide and the counterions present in the solution.

Figure 5 shows the schematic representation of two possible scenarios of multilayer formation. The cylinders represent the melittin molecules. In Figure 5a, melittin tetramers, which were formed in solution, bound directly to the phospholipid membrane, which resulted in multilayers (double layers) on the surface. In Figure 5b, although at higher melittin concentrations tetramers existed in solution, only monomers bound to the surface, forming multilayers. Data on multilayer formation of melittin on solid-supported POPC membranes, especially the small calculated surface charge density \( \sigma \) in the range \( 0–12 \text{mC·m}^{-2} \), was too small to avoid coalescence, in agreement with the evidence for multilayer formation of melittin on solid-supported phospholipid membranes by shear-wave resonator measurements.
The local microenvironment composition of the lipid bilayer played a role as a regulator of the cross-linking activity of melittin and other toxins. In anionic phospholipid bilayers, its physical state gel or liquid crystal had no effect on melittin binding, contrary to neutral lipids, which showed that electrostatic forces played a role in the formation of the complex, and ruled out a penetration of the hydrophobic part of the peptide in the bilayer. The conclusion is supported by the fact that the stoichiometry of complexes was related to the surface charge density of the bilayer, as shown by pH effects on dimyristoylphosphatidic acid. The physical state of the bilayer and hydrophobic force played a role in the interaction with the toxins. However, at variance to neutral membranes, the driving force was modulated by electrostatic interactions, which controlled the phase formation below or above the temperature of gel-to-fluid transition. In addition to the interest in cell membranes and phospholipid bilayers, motivation exists for the design of supported membrane biosensors for medical and pharmaceutical applications. Assuming a certain structure for colloidal gels, a simple but systematic scaling theory was derived for storage modulus and limit of linearity of colloidal gels that were above the gelation threshold. The scaling of the elastic properties of colloidal gels resulted dominated by the fractal nature of the flocs and different from the scaling near the gelation threshold, where a percolation-type scaling applied. The exponents for storage modulus and limit of linearity were expressed in terms of flocks and backbone fractal dimensions. Flocks fractal dimension resulted that of the colloidal aggregates. Two types of scaling behaviour existed: strong- and weak-link regimes. The scaling of the storage modulus and limit of linearity depended on whether the interfloc links were stronger than the flocks. The linear region shrank with the rising concentration in the strong-link regime but rose with the rising concentration in the weak-link scheme. The theory enabled extracting, from the rheological measurements, structural information about the individual flocks. The fractal dimension of the microstructural net of a fat crystal net is an indicator of the storage modulus of the net and hardness of the fat crystal net. The fractal and fractal backbone dimensions were calculated from polarized light microscope images of the net. The AMPs showed in vitro activity vs. micro-organisms resistant to conventional antibiotics. Their most common mode of action was the disruption of cell membranes leading to microbial lysis, which presented lesser risk of acquired resistance or cross-resistance with other agents than other modes, which made it an attractive template for the design of antimicrobials for specific applications. The outmost leaflets of the bilayer, which is exposed to the outside of the anionic bacterial membranes, are more attractive to the attack of cationic AMPs. The interaction is...
mainly electrostatic actions, which are the major driving forces for cellular association. A need exists for modernizing the statistical methods used in research. Statistical modelling is improving. One cannot be an expert in everything; however, one can be encircled by experts. Is statistics a noble branch of esoteric sciences or an instrument to clarify a phenomenon existing behind data? Is the statistician a being nonplussed to a computer or an active collaborator integrated into a research team? New statistical methods allow to get more robustness in the conclusions and extract more information from the data.

CONCLUSION

From the previous results and discussion, the following conclusions can be drawn.

1. According to the Derjaguin–Landau–Verwey–Overbeek model, the energy well corresponding to melittin aggregation in membranes was rather broad and, practically, no barrier exists opposing the aggregation of melittin molecules. Such aggregation corresponds to a small energy variation relative to thermal energy, which suggested that spontaneous thermal fluctuations affected melittin aggregation state at membrane/solution interface. The adsorption was treated via Langmuir adsorption isotherm modified with electrostatic effects. The theoretical treatment was an elegant method, because the two Gouy–Chapman and Debye–Hückel formalisms applied the same Poisson–Boltzmann equation to calculate either potential.

2. The results made evident the formation of the melittin multilayer on the phospholipid membranes. Melittin tetramers, which were formed in solution, bound directly to the phospholipid membrane, which resulted in multilayers on the surface. Work is in progress on testing the utility of steady-state spectrofluorimetry, Förster resonance energy transfer, fluorescence anisotropy and polarization, total internal reflection fluorescence, circular dichroism, circular-dichroic stopped-flow, polarimetry, Raman spectroscopy, polarized and attenuated total reflection Fourier-transform infrared spectroscopy, infrared dichroism, sum frequency generation vibrational spectroscopy, $^{31}$P, $^{13}$C, $^1$H, $^2$H, spin label, solid-state, nuclear-Overhauser, photochemically induced dynamic-nuclear-polarization and heteronuclear single-quanta coherence nuclear magnetic resonance, electron spin-echo envelope modulation and resonance spectroscopy, quasi-elastic light scattering, thin-layer, reverse-phase and size-exclusion high-performance liquid chromatography, X-ray diffractometry, X-rays and neutron off-plane scattering, electron and confocal microscopy, high-sensitivity differential scanning calorimetry, temperature scanning densitometry, conductance, viscometry, ultracentrifugation, quartz crystal microbalance, lateral diffusion measurements, imaging ellipsometry, reflection interference contrast microscopy, enzymatic cleavage experiments, cytolitic and haemolytic activity assays, assay of antibacterial activity of the peptides, fractal dimension analysis, molecular dynamics simulations, molecular modelling and computer analysis to confirm the present outcomes.

3. Further work will give a better quantitative description of the association isotherms at higher ionic strength and improve the approach in anionic lipid membranes. Although melittin enlightened its behaviour in the presence of natural membranes, it still remains to settle more definitively the parallelism between its perturbation induced on lipids and cell membranes. What is the detailed structure
of the detected soluble complexes? To which extent are they involved in the mechanism of action of cytolytic toxins?

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LITERATURE CITED


